

## 波動率曲線編製說明

### Exponentially Weighted Moving Average Volatilities

Date:		Exponentially Weighted Moving Average Volatilities													
Decay factor		0.9 <span style="color: cyan;">→ i</span>													
		1m	3m	6m	1yr	2yr	3yr	4yr	5yr	7yr	9yr	10yr	15yr	20yr	30yr
Yield Volatility (%)	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$	$B_i$
Current Yield (%)	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$	$A_i$
Price Volatility (%)	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$	$C_i$
Correlation Matrix	$j$	1													
	1m														
	3m	1													
	6m		1												
	1yr			1											
	2yr				1										
	3yr					1									
	4yr						1								
	5yr							1							
	7yr								1						
	9yr									1					
	10yr										1				
	15yr											1			
	20yr												1		
	30yr													1	

$A_i$  : 每日的 Cubic B-Spline 模型的該期間零息利率

$$B_i : B_i = \sqrt{\sigma_i^2 \times 250}$$

其中：

$$\sigma_i^2 = \lambda \sigma_{i-1}^2 + (1 - \lambda) r_i^2$$

$$r_i = \ln \frac{A_i}{A_{i-1}}$$

$$\lambda = \text{Decay factor}(0.90, 0.91, 0.92, \dots, 0.99)$$

$$C_i : C_i = \sqrt{S_i^2 \times 250}$$

其中：

$$S_i^2 = \lambda S_{i-1}^2 + (1 - \lambda) R_i^2$$

$$R_i = (-i) \times \ln \left( \frac{1 + A_i}{1 + A_{i-1}} \right) \quad , i = 1m, 3m, 6m, \dots, 30Yr, i \text{ 及 } j \text{ 以年為單位}$$

$$\lambda = \text{Decay factor}(0.90, 0.91, 0.92, \dots, 0.99)$$

$$D_{i,j} : D_{i,j} = \frac{S_{ij}}{S_i \times S_j}$$

其中：

$$S_{i,j} = \lambda S_{i,j-1} + (1 - \lambda) R_i \cdot R_j$$

## Equally Weighted Moving Average Volatilities

Equally Weighted Moving Average Volatilities															
Date:2007/4/17	$i$ →														
Days of historical data	62														
	1m	3m	6m	1yr	2yr	3yr	4yr	5yr	7yr	9yr	10yr	15yr	20yr	30yr	
Yield Volatility (%)	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	$b_j$	
Current Yield (%)	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	$a_j$	
Price Volatility (%)	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	$c_j$	
Correlation Matrix	1m	3m	6m	1yr	2yr	3yr	4yr	5yr	7yr	9yr	10yr	15yr	20yr	30yr	
	1														
		1													
			1												
				1											
					1										
						1									
							1								
								1							
									1						
										1					
											1				
												1			
													1		
														1	
															1

$a_j$  : 每日的 Cubic B-Spline 模型的該期間零息利率

$$b_j : b_i = \sqrt{\sigma_i^2 \times 250}$$

其中：

$$\sigma_i^2 = \frac{1}{T} \sum_{n=0}^{T-1} r_{i,-n}^2$$

$$r_{i,-n} = \ln \frac{a_{i,-n}}{a_{i,-n-1}}$$

$$T = \text{Days of historical data} \quad (62 \text{ or } 125 \text{ or } 250)$$

$$c_j : c_i = \sqrt{S_i^2 \times 250}$$

其中：

$$S_i^2 = \frac{1}{T} \sum_{n=0}^{T-1} R_{i,-n}^2$$

$$R_{i,-n} = (-i) \times \ln \left( \frac{1+a_{i,-n}}{1+a_{i,-n-1}} \right) \quad , i = 1m, 3m, 6m, \dots, 30Yr, i \text{ 及 } j \text{ 以年為單位}$$

$$T = \text{Days of historical data} \quad (62 \text{ or } 125 \text{ or } 250)$$

$$d_j : d_{i,j} = \frac{S_{ij}}{S_i \times S_j}$$

其中：

$$S_{ij} = \frac{1}{T} \sum_{n=0}^{T-1} (R_{i,-n} \times R_{j,-n})$$

$$T = \text{Days of historical data} \quad (62 \text{ or } 125 \text{ or } 250)$$